TABLE IV

le:

The $2p$ -level $(N=2, l=1)$			
n	E atomic units	atomic units	from section
2	-0.1250	000	3a
2.047	-0.1193	10.235	36
2.135	0.1097	8.540	36
2.363	-0.0895	7.089	36
2.5	-0.0800	6.701	36
2.599	0.0740	6.497	36
3	-0.0566	6.000	3a
3.5	0.0408	5.696	3 <i>b</i>
4	-0.0312	5.528	3a
5	-0.0200	5.355	3a
00	0	5.086	3c
4 i	0.0312	4.770	3d
3 i	0.0556	4.554	3d
2 i	0.1250	4.110	3d
i	0.5000	2.698	3d
0.778 i	0.8261	2.528	3d
0.445 i	2.524	1.68	3j
0.401 1	3.116	1.55	3 <i>f</i>
0.356i	3.943	1.41	31
0 i	∞	0	3e

n-l-1 nodes between the points r=0 and $r=\infty$. For several values of n and for l=0 and 1 zero points have been calculated and given in tables II–IV (indication § 3a) and represented in the figures 1–3. Here again the splitting up of the second level into 2s and 2p curves is evident. It is obvious that by using only integer values of n a large gap in the curves is left between n=l+1 and n=l+2 i.e. between $r_0=\infty$ and a comparatively small value of r_0 . On the side of large radii r_0 this gap could be filled by the method of § 2, but this gives only approximative values.

b) For the rest of the gap in the curve it is necessary to find zero points of the confluent hypergeometric function with real arguments. These can be interpolated from tables ⁶) ⁷) with the help of well-known interpolation procedures (v. tables II-IV and figures).

c) E=0. The limiting case of $n\to\infty$ has been studied by Sommerfeld and Welker²), especially for the 1s level. The confluent hypergeometric function (6) for $n\to\infty$ is proportional to a Bessel function:

$$\lim_{n \to \infty} F(l+1-n, 2l+2, \varrho) \propto J_{2l+1}(2\sqrt{\varrho n}) = J_{2l+1}(2\sqrt{2r}). \tag{24}$$